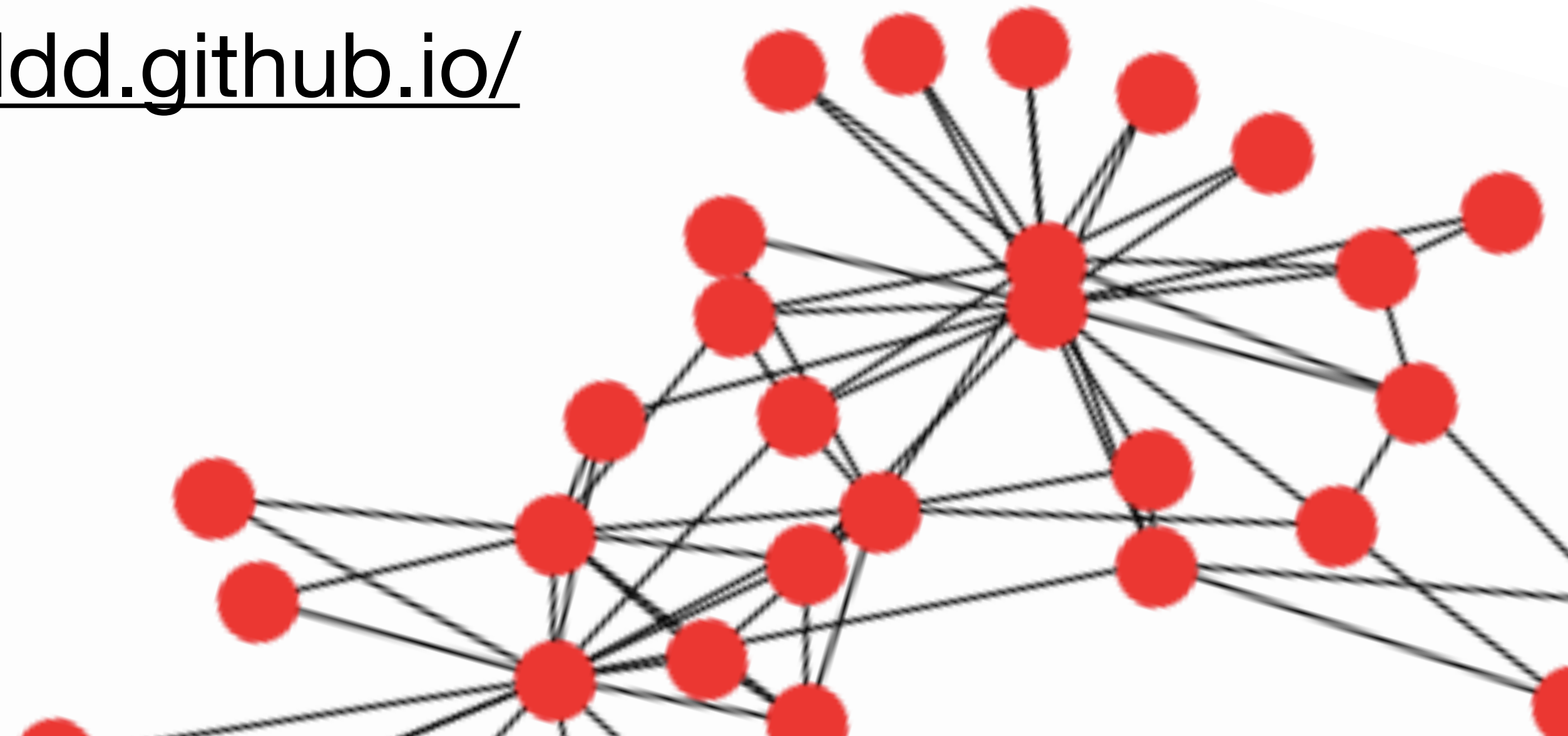


# Week 8: Cascades/CW Tutorial

Naomi Arnold

<https://narnolddd.github.io/>



# Tutorial aims

- **Recap** the cascades lecture
- **Go over** a cascade threshold example
- **Get some pointers for** where to start with the network analysis coursework, with Gephi demo
- If **time\_left > 0**, answer some coursework questions

# What can be modelled as a cascade?



**Movements to change  
a consensus**



**Uptake of new  
technologies/products**

# Important features

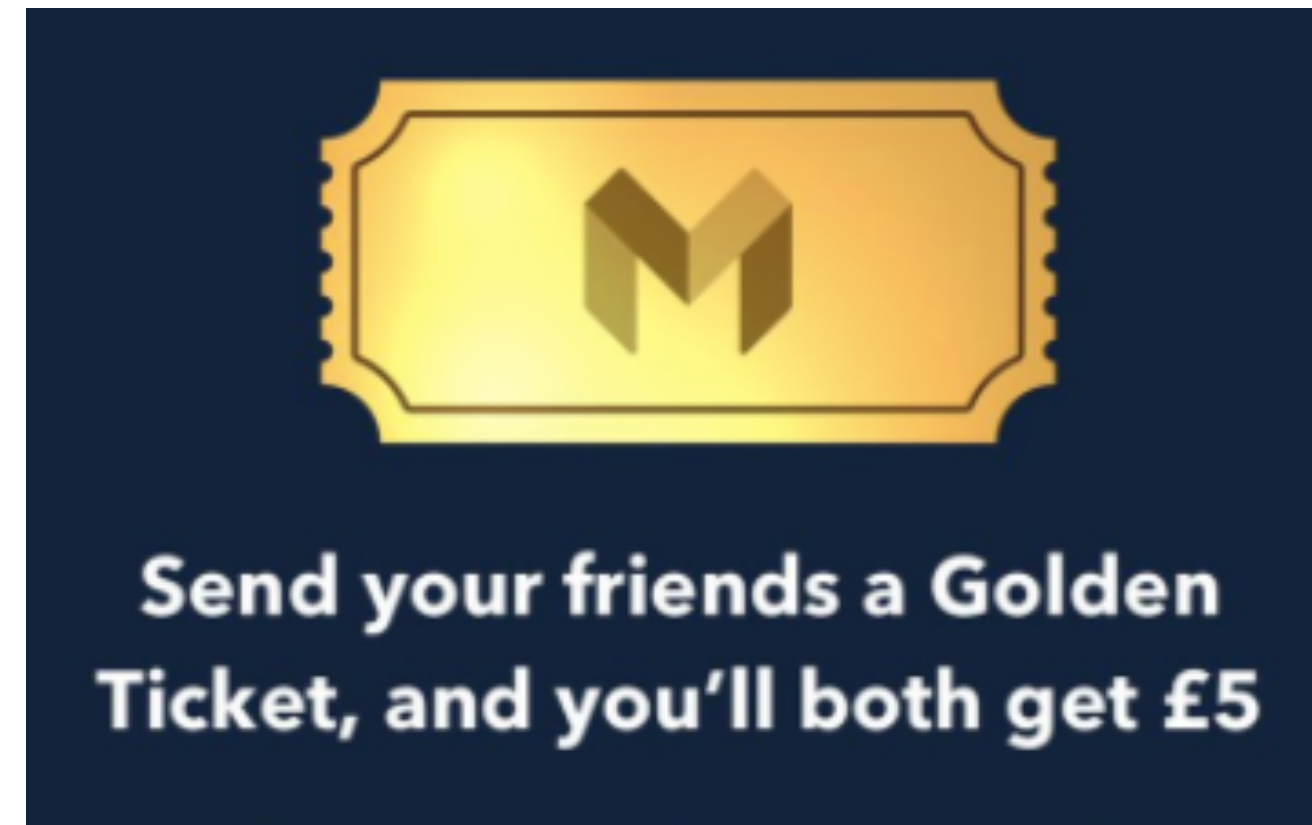
- Each agent (node) is in **one of two states** — adopter or non-adopter
- **State** of a node depends only on that of its **neighbours**. I.e. grass-roots and no outside influence
- Each node acts **rationally**

# Game-theoretic formulation

- Pair of nodes  $v$  and  $w$  in a social graph
- Behaviours  $A$  and  $B$
- If both adopt  $A$ , they each get a payoff  $a > 0$
- If both adopt  $B$ , they each get a payoff  $b > 0$
- If they adopt **opposite** behaviour, both get a payoff of 0

		$w$	
		$A$	$B$
$v$	$A$	$a, a$	$0, 0$
	$B$	$0, 0$	$b, b$

# What can payoff mean?



(Monzo bank scheme)

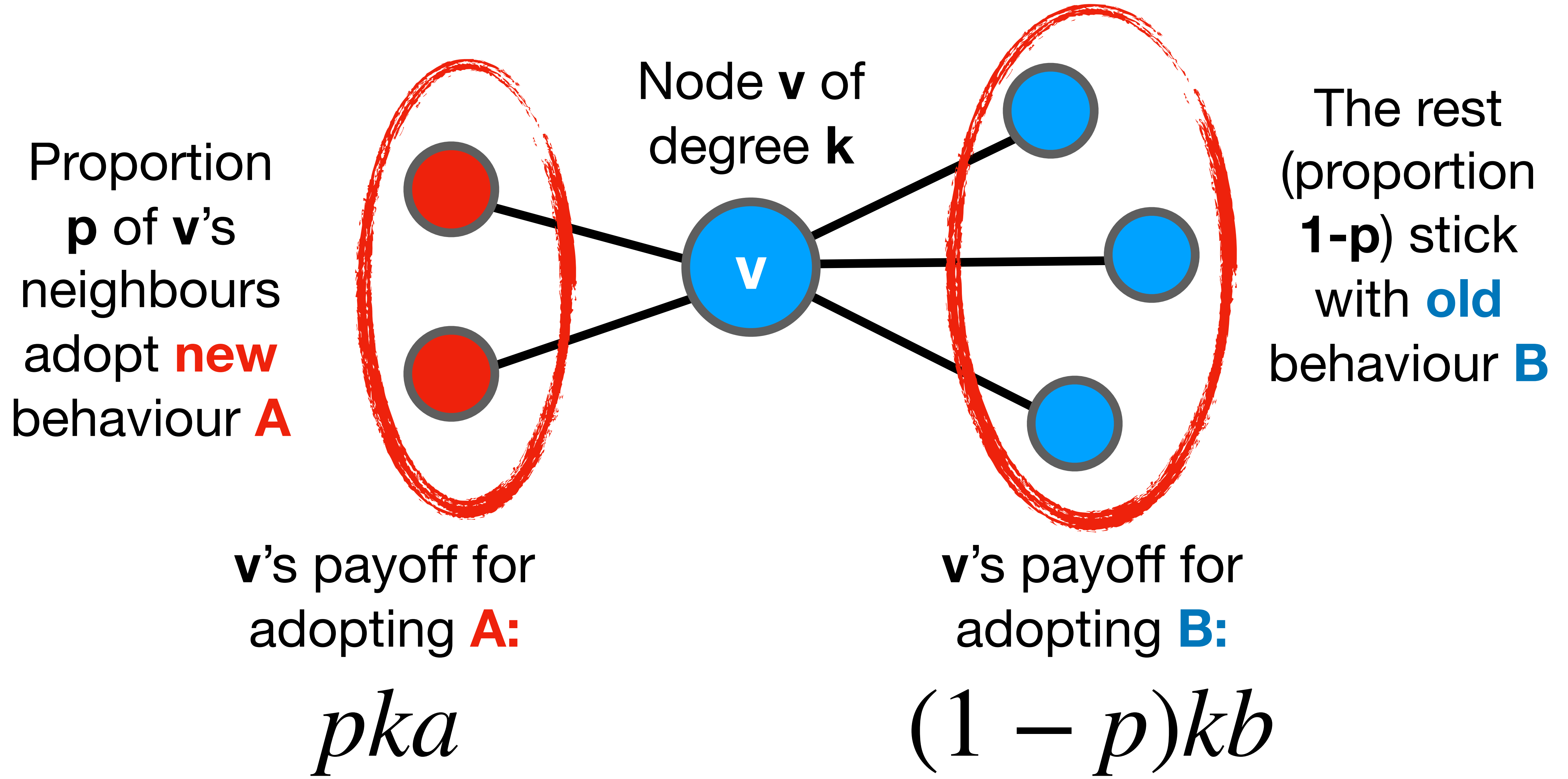


**Social cohesion:** easier (maybe!) to be friends with someone you agree with on something

**Literal cash:** Receive incentives for adopting or encouraging others to adopt

**Other benefits:** using same technologies/platforms

# Cascade threshold



# Cascade threshold

Adopting new behaviour  
**A** is a better\* option if:

$$pka \geq (1 - p)kb$$
$$p \geq \frac{b}{a + b}$$

\*assuming nodes are rational and want option with best payoff — not always the case in reality!!



# Cascade threshold

Adopting new behaviour  
**A** is a better\* option if:

$$pka \geq (1 - p)kb$$

$$p \geq \frac{b}{a + b}$$

**Cascade threshold** — proportion of  
neighbours you need to **convince** you  
to adopt behaviour **A!**

\*assuming nodes are rational and want option with best payoff — not always the case in reality!!

# Cascade threshold interpretation

**Small threshold**

**$< 1/2$**

**New behaviour appealing, little convincing needed**

**Threshold equal to**

**$1/2$**

**People will simply follow majority of their friends**

**High threshold**

**$> 1/2$**

**New behaviour less appealing, need critical mass of initial adopters**

# Example

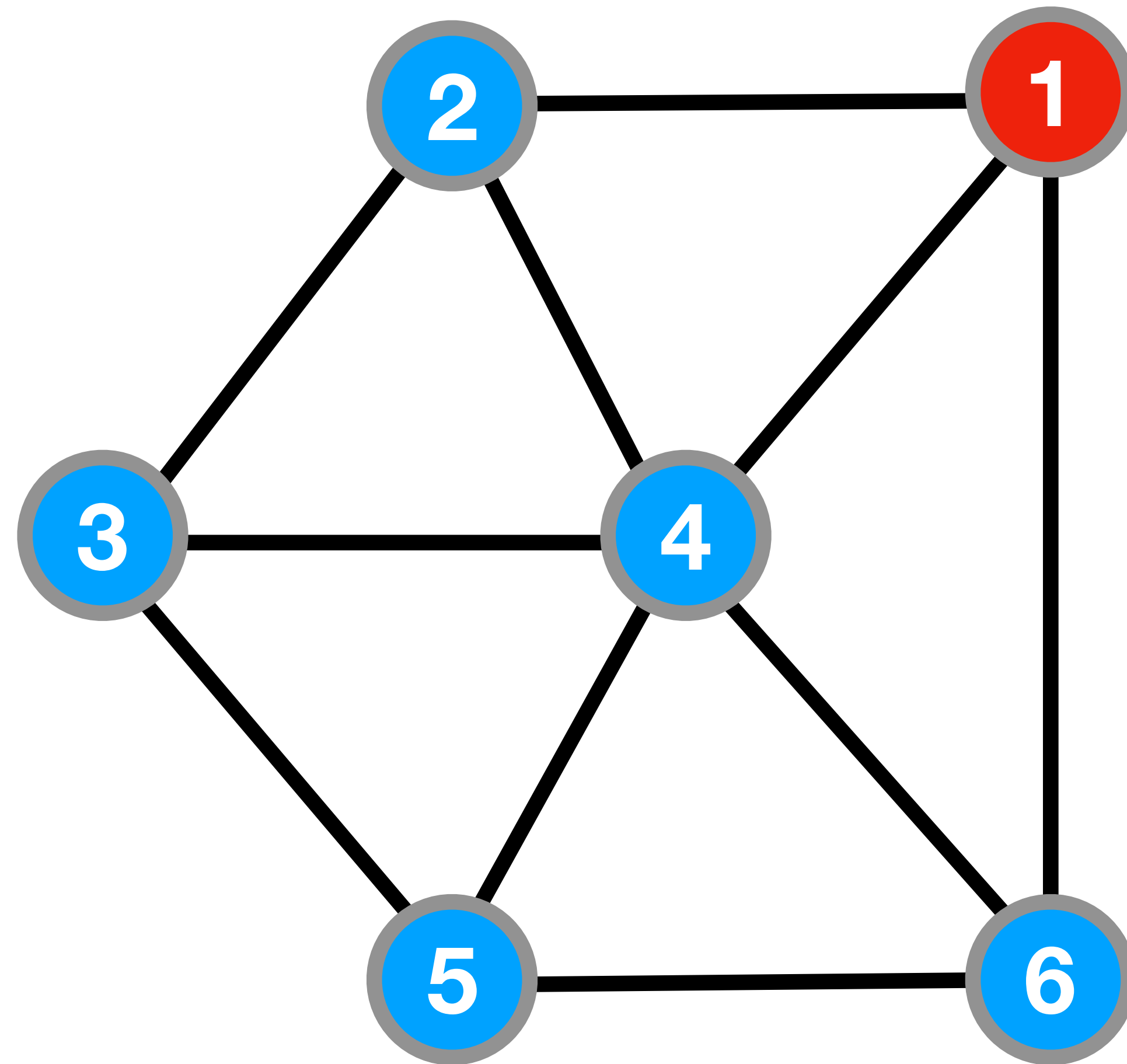
$$a = 3, b = 1$$

**Threshold**

$$= b/(a+b)$$

$$= 1/(1+4)$$

$$= 1/4$$



# Example

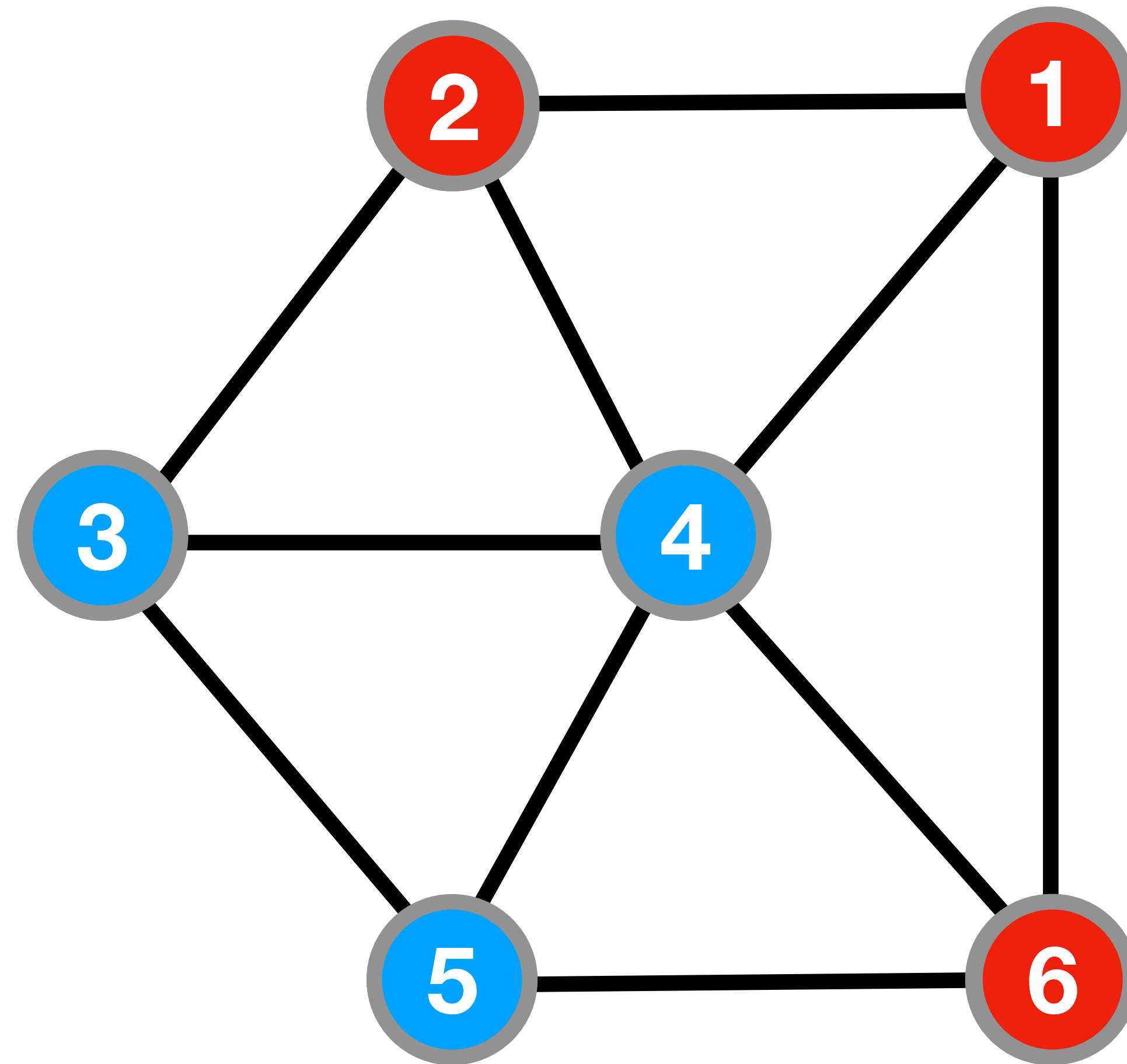
$$a = 3, b = 1$$

**Threshold**

$$= b/(a+b)$$

$$= 1/(1+4)$$

$$= 1/4$$



# Example

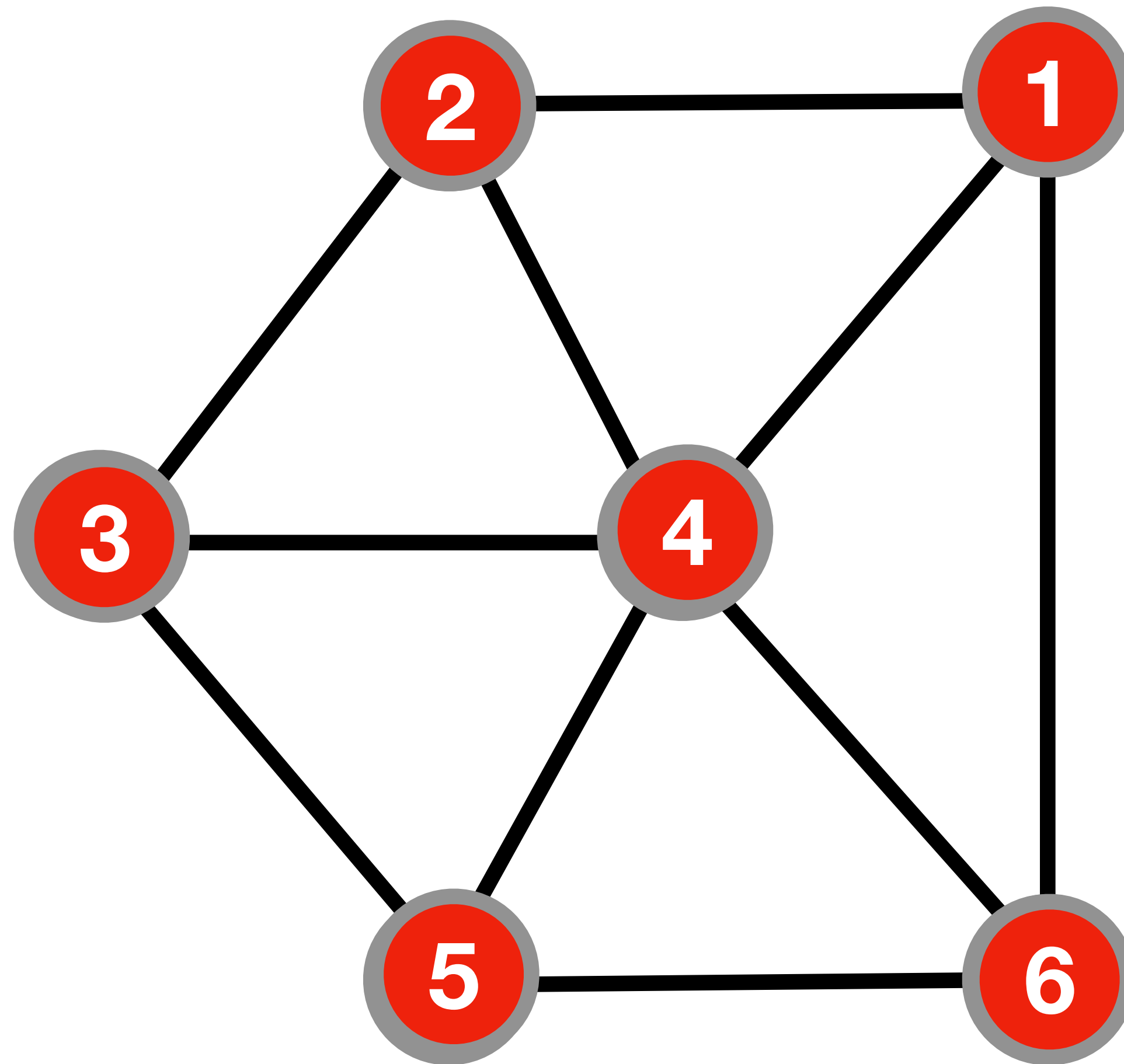
$$a = 3, b = 1$$

**Threshold**

$$= b/(a+b)$$

$$= 1/(1+4)$$

$$= 1/4$$



# Example

$$a = 3, b = 1$$

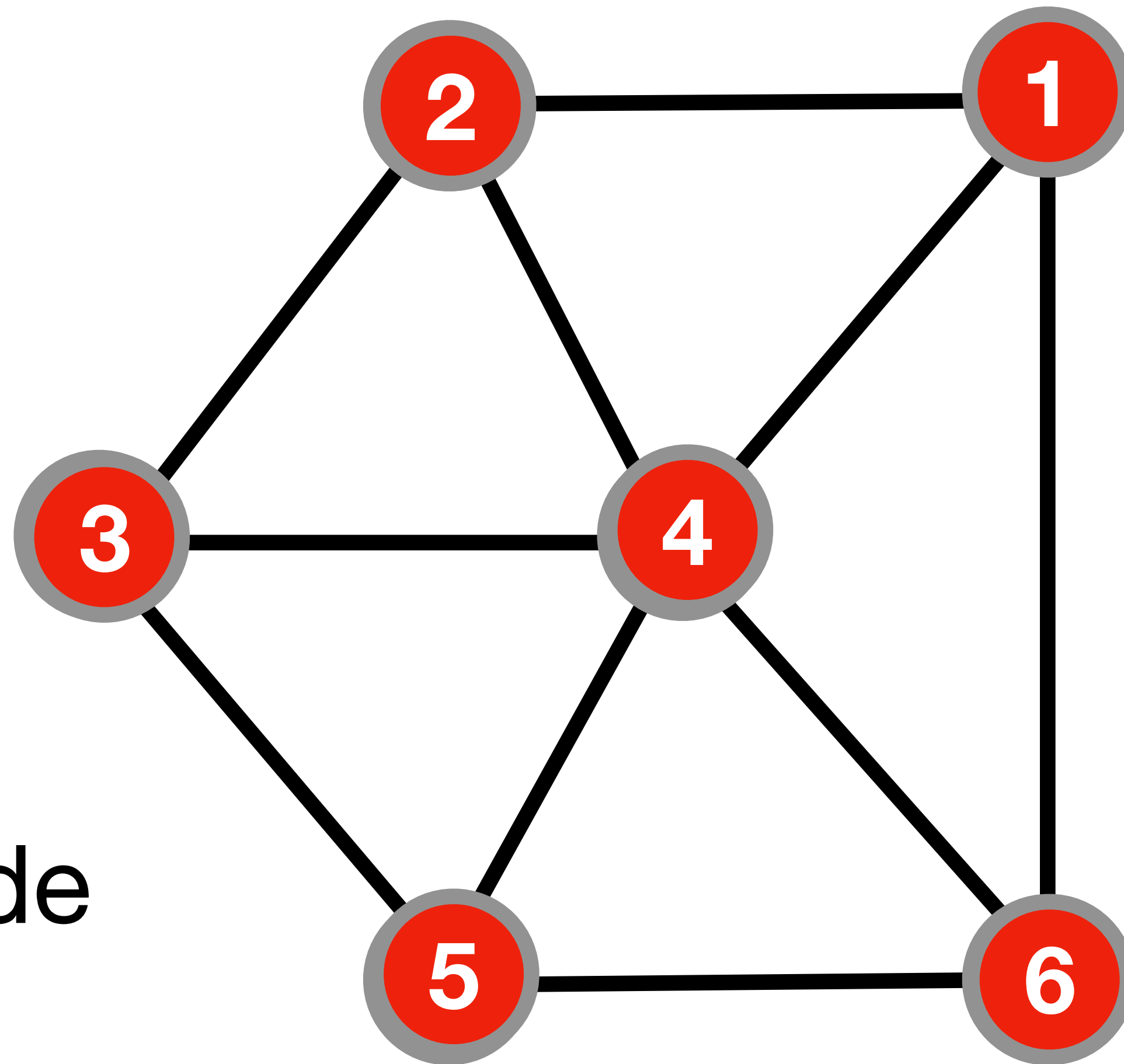
**Threshold**

$$= b/(a+b)$$

$$= 1/(1+4)$$

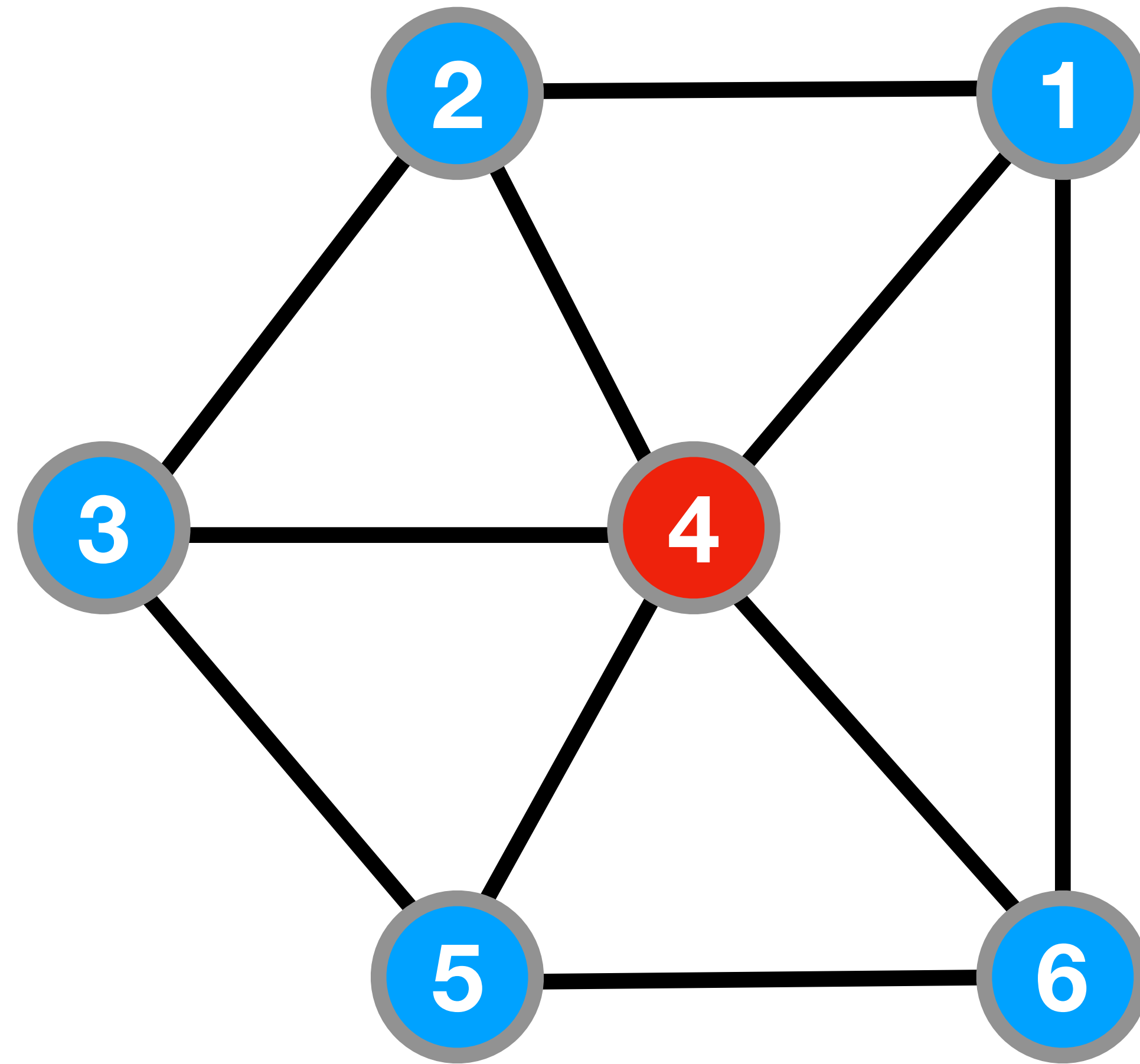
$$= 1/4$$

Leads to **complete cascade**



# Example

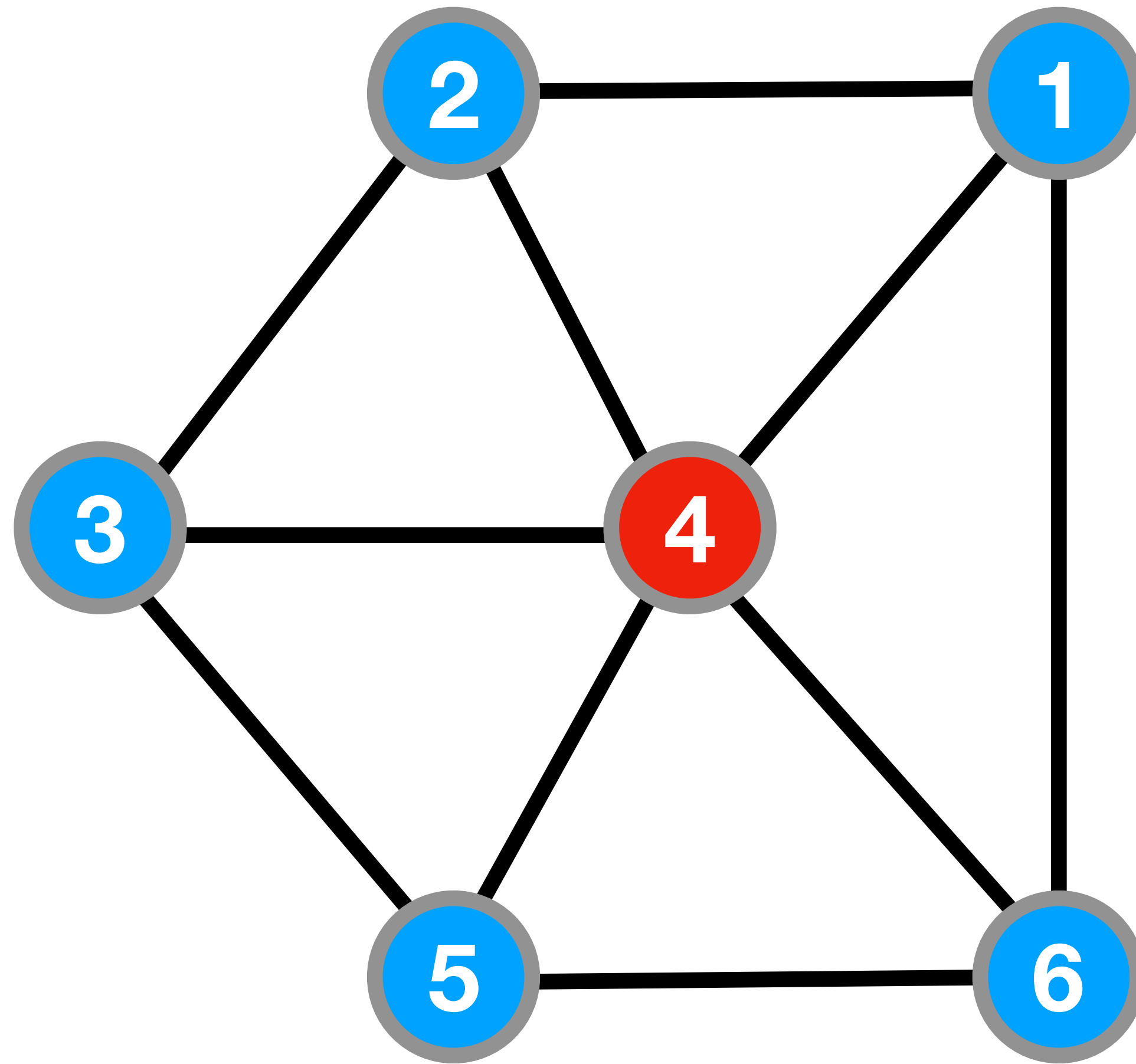
**What threshold would you need to generate a cascade from this node?**



# Example

**What threshold would you need to generate a cascade from this node?**

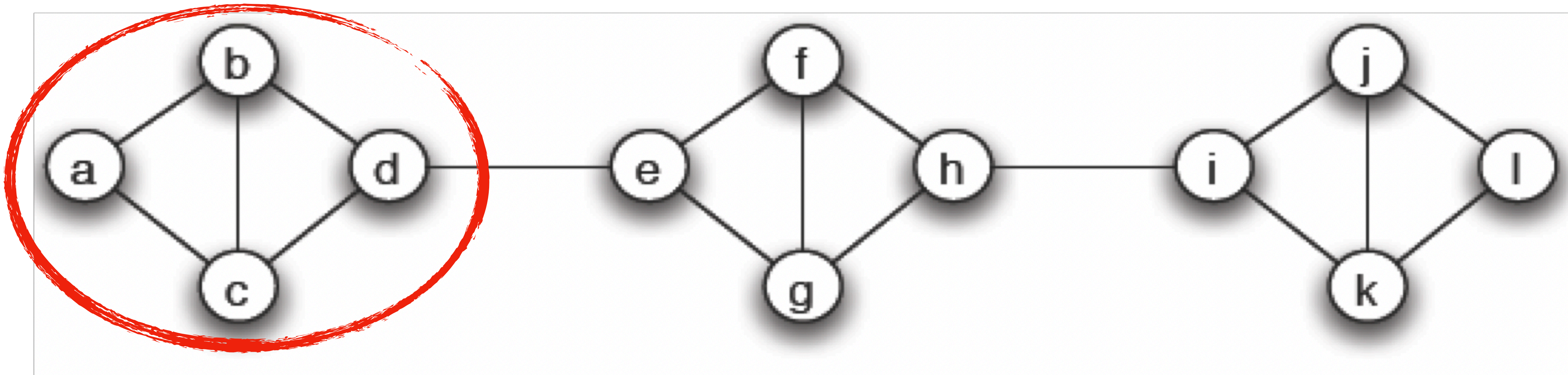
Each neighbour has degree **3**, so anything lower than  **$1/3$**  will generate cascade





# Effects of network structure

**Weak ties between tightly clustered communities **stop** cascades**



Cascade threshold would need to be **lower than 1/3**  
for **e** to be convinced to **pick up new behaviour**

# Studying systems as networks

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## System of interest

e.g. the Internet, the human brain,  
Twitter, real social networks

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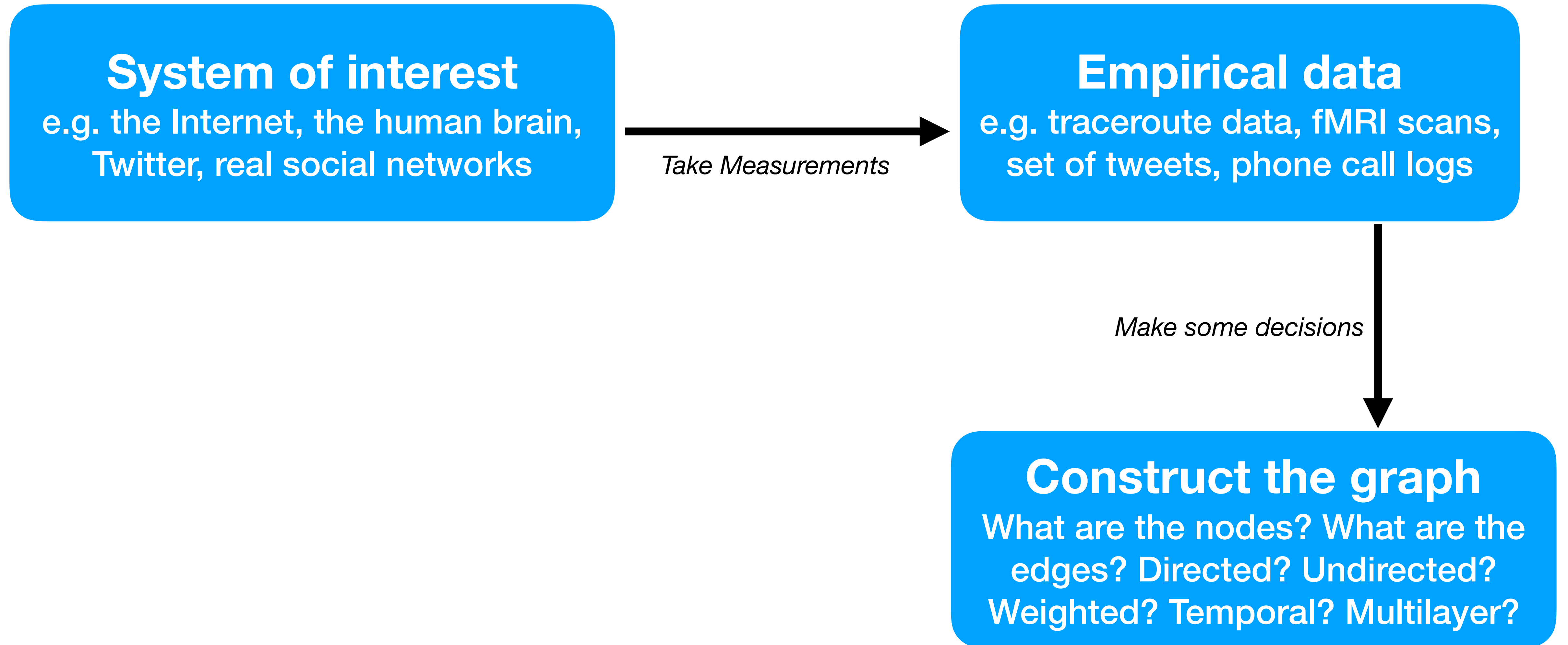


*Take Measurements*

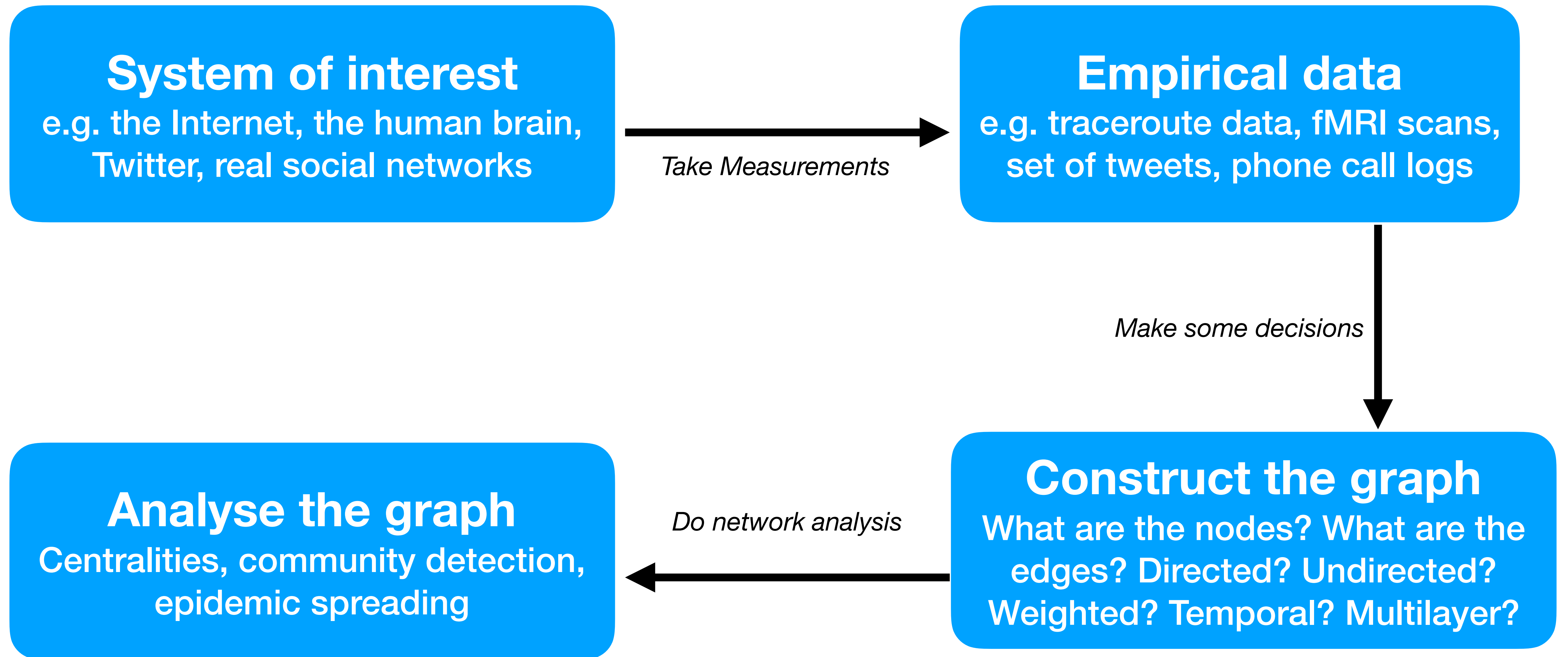
## Empirical data

e.g. traceroute data, fMRI scans,  
set of tweets, phone call logs

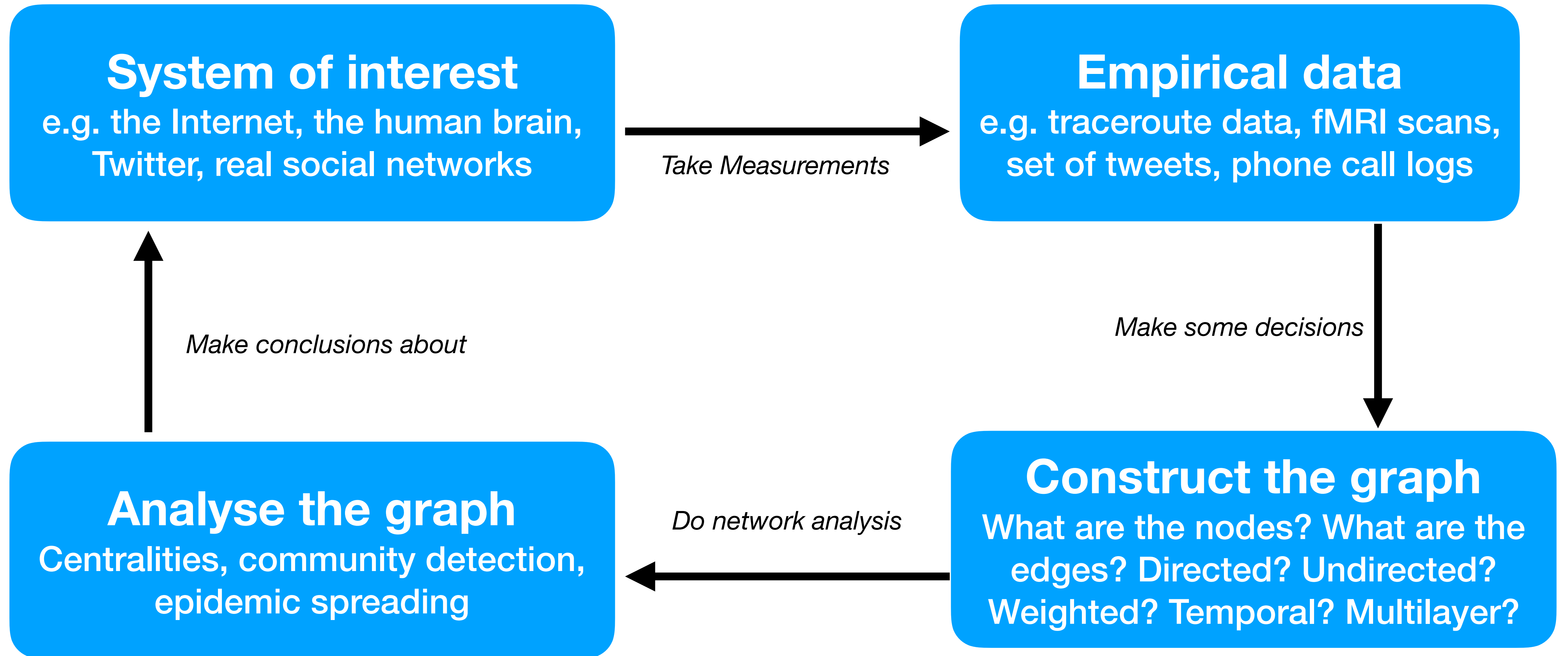
# Studying systems as networks



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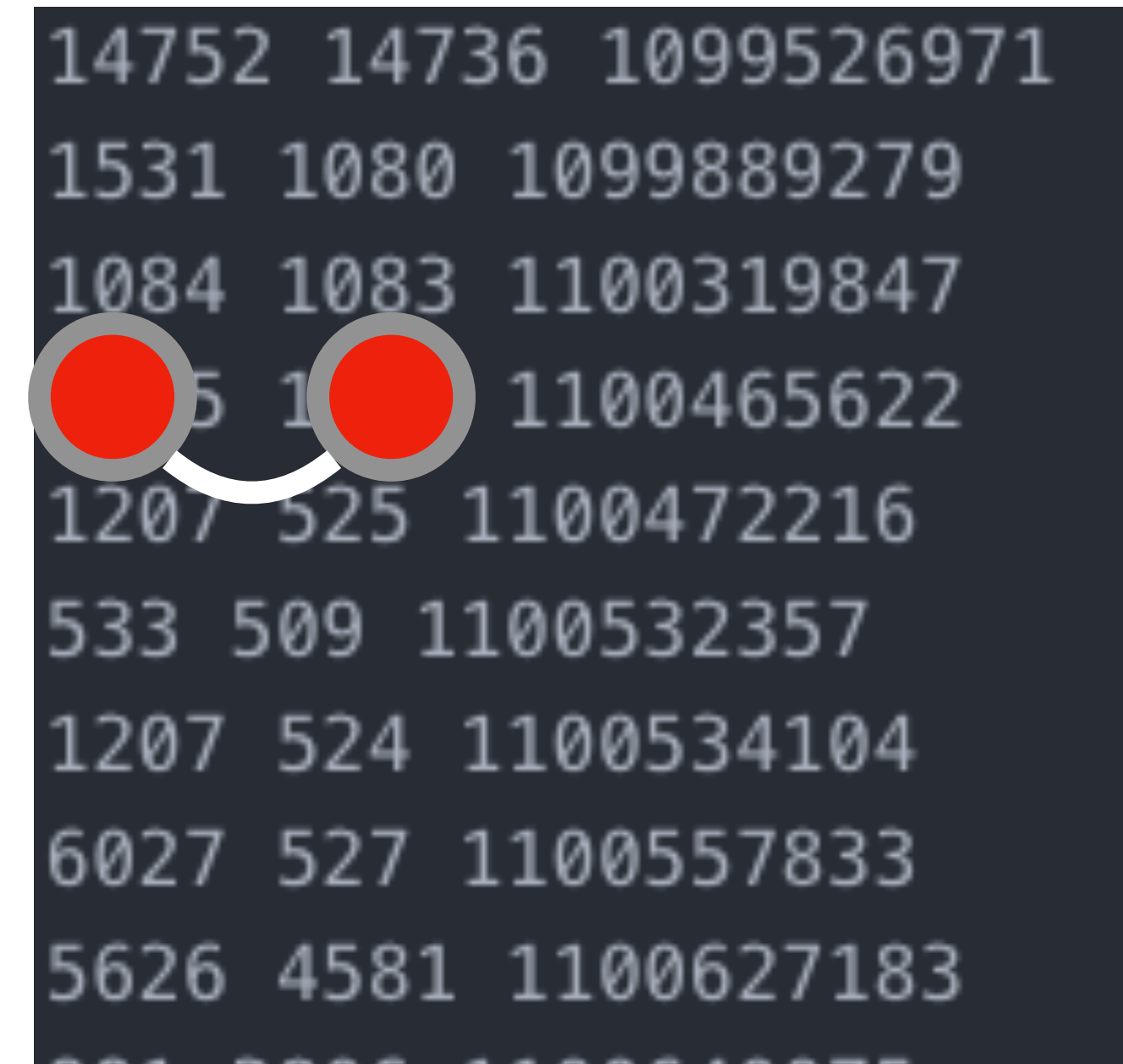


# Studying systems as networks



# Data Types: Edge List

- Usually a list with each row having **2 or more** comma/tab separated values
- First two values are **source** and **destination** nodes of edge
- Any extra values are **metadata** e.g. timestamp, edge weight



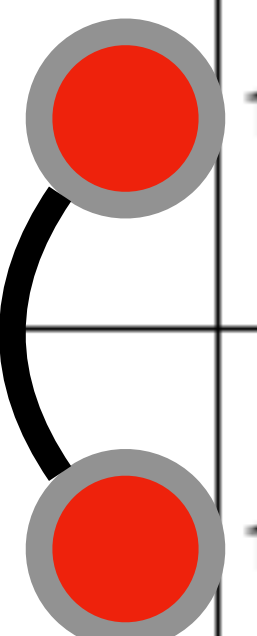
```
14752 14736 1099526971
1531 1080 1099889279
1084 1083 1100319847
5 1 1100465622
1207 525 1100472216
533 509 1100532357
1207 524 1100534104
6027 527 1100557833
5626 4581 1100627183
884 2886 1100648875
```

e.g. Facebook wall post dataset has user ids of wall poster and postee resp., and UNIX timestamp of when post was created



# Data types: Databases

eventName	eventSec	id	matchId	matchPeriod	playerId	positions	subEventId	subEventName	tags
Pass	1.656214	258612104	2057954	1H	122671	[[{'y': 50, 'x': 50}, {'y': 53, 'x': 35}]]	85	Simple pass	['id': 1801]
Pass	4.487814	258612106	2057954	1H	139393	[[{'y': 53, 'x': 35}, {'y': 19, 'x': 75}]]	83	High pass	['id': 1801]
Duel	5.937411	258612077	2057954	1H	103668	[[{'y': 81, 'x': 25}, {'y': 83, 'x': 37}]]	10	Air duel	['id': 703, 'id': 1801]

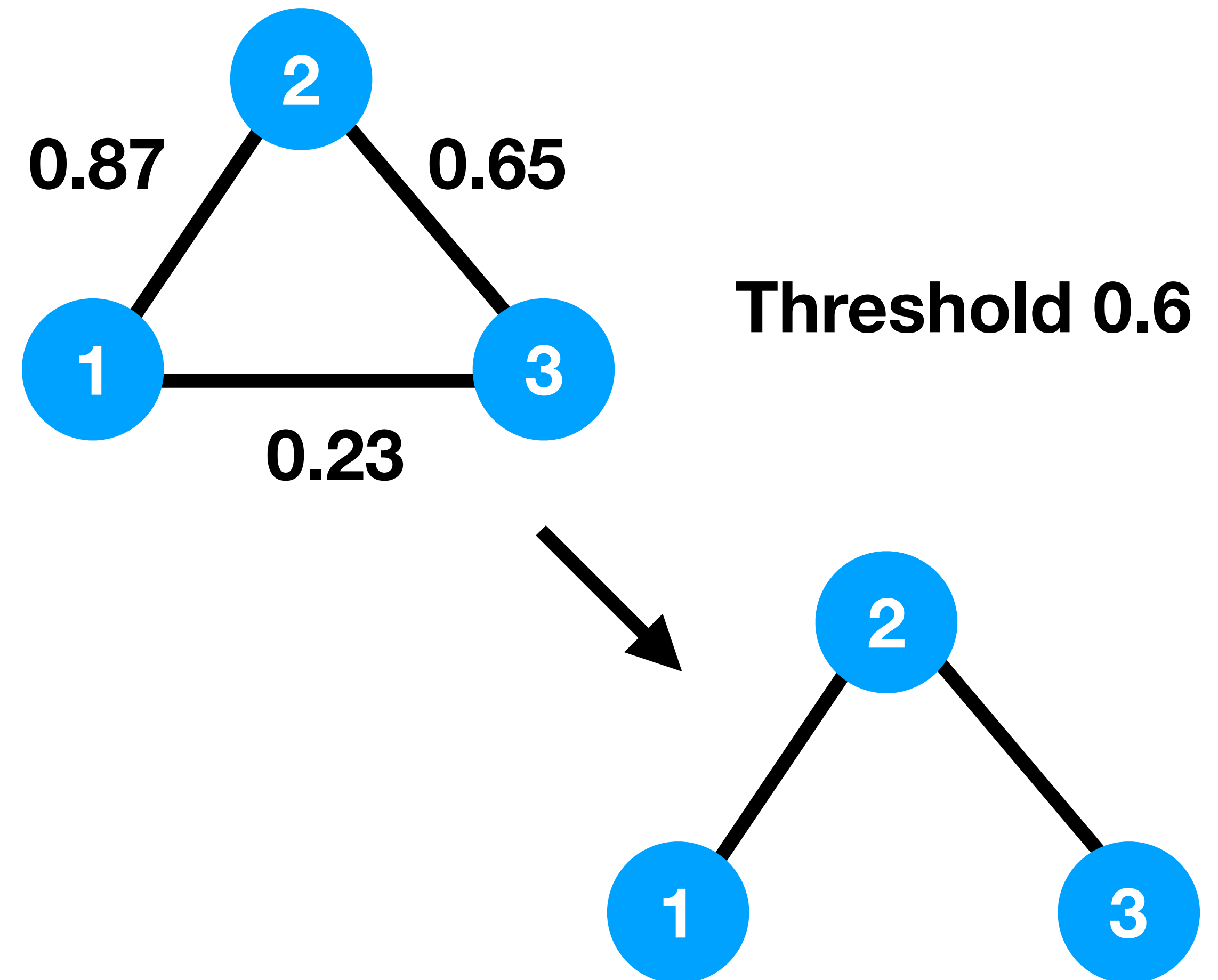


**More complicated example: FIFA dataset where edges could be passes, specific types of passes, tackles etc.**

# Data Types: Adjacency/Weight Matrix

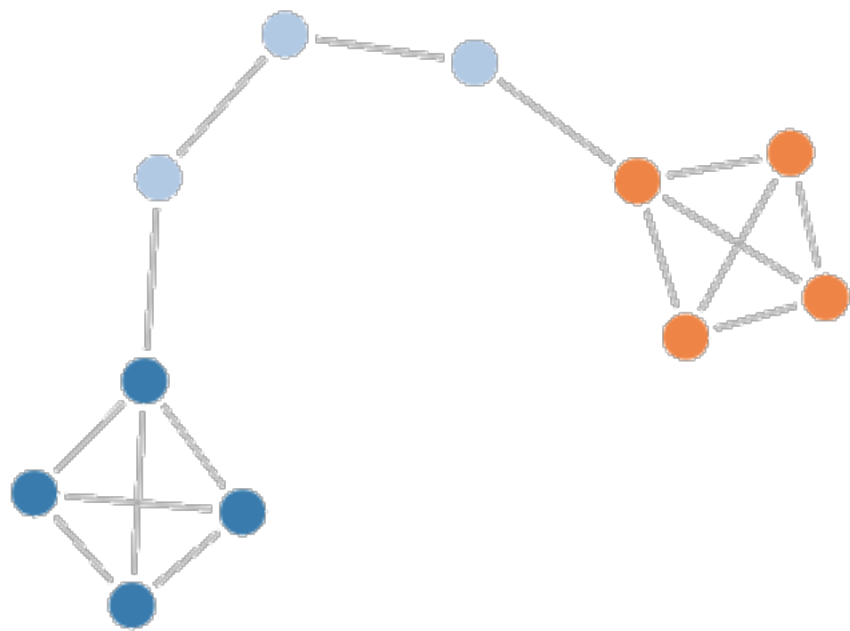
**Dest Node**

	1	2	3
<b>Source Node</b> 1	0	0.87	0.23
2	0.87	0	0.65
3	0.23	0.65	0

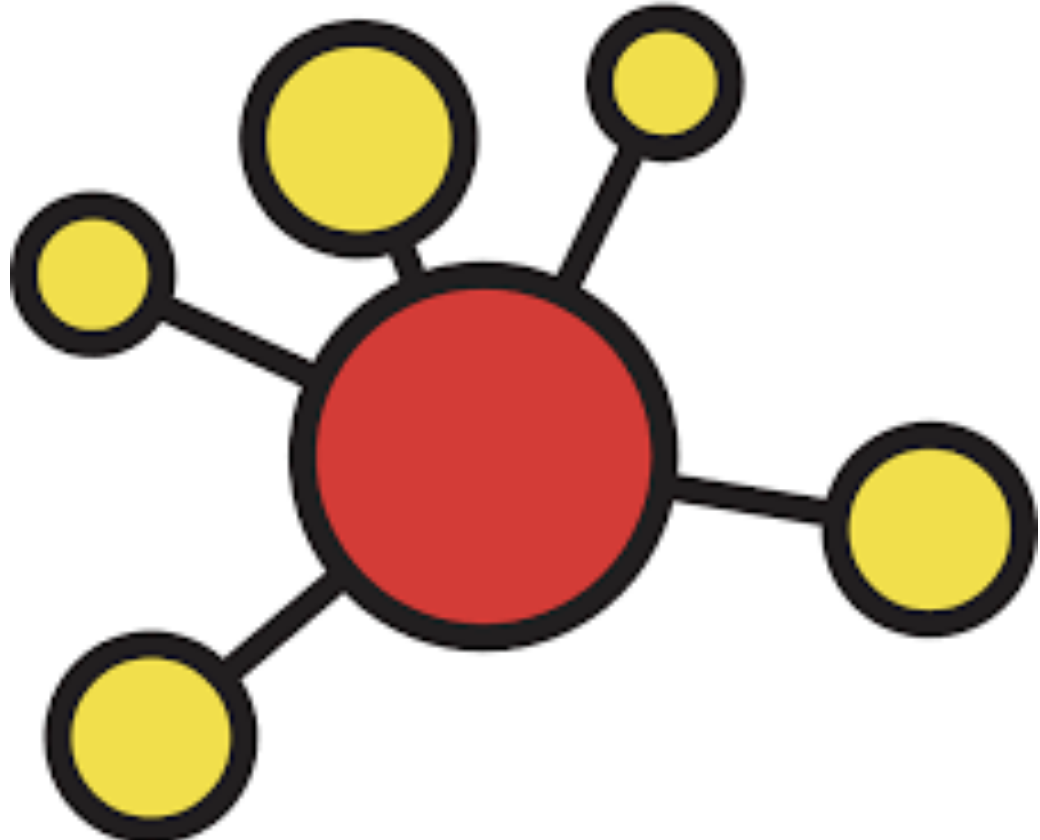


Value at **row i** and **column j** is the weight between node i and j

# Software/libraries for network visualisation



**NetworkX**



**(iGraph)**

*Gephi* Gephi

# Aaagh, my network is too big — thinning

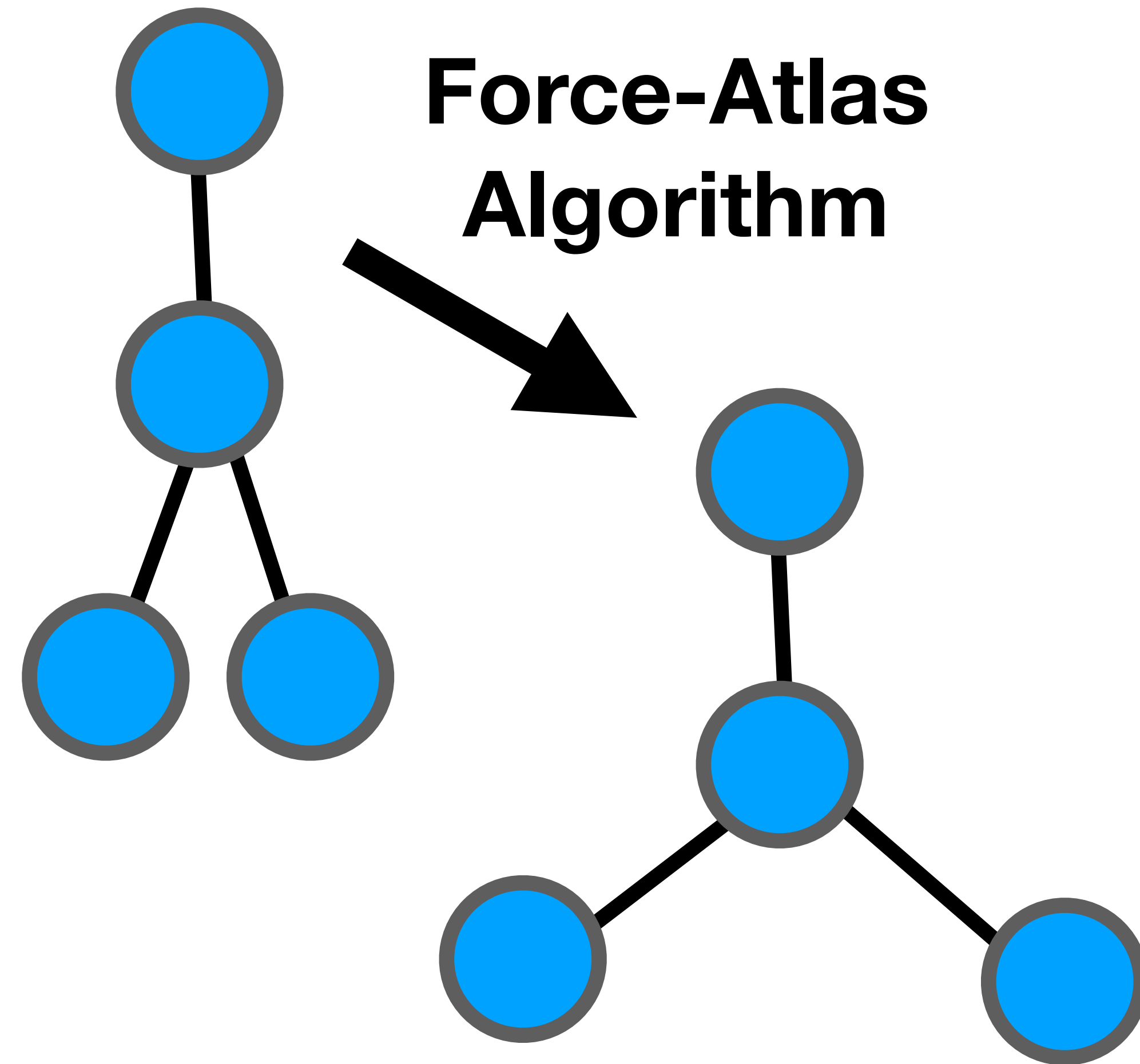
- **Windowing** — if the edges in your dataset have timestamps, look only at edges within a certain time window.
- **Random edge sample** (requires preprocessing in e.g. Python) — take a random sample of the edges in the dataset.
- **Random node sample** — take the network you get from a random sample of the nodes
- **Degree filter** — only include nodes of above a certain degree (e.g. get rid of nodes of degree 0,1)

# Network visualisation ingredients

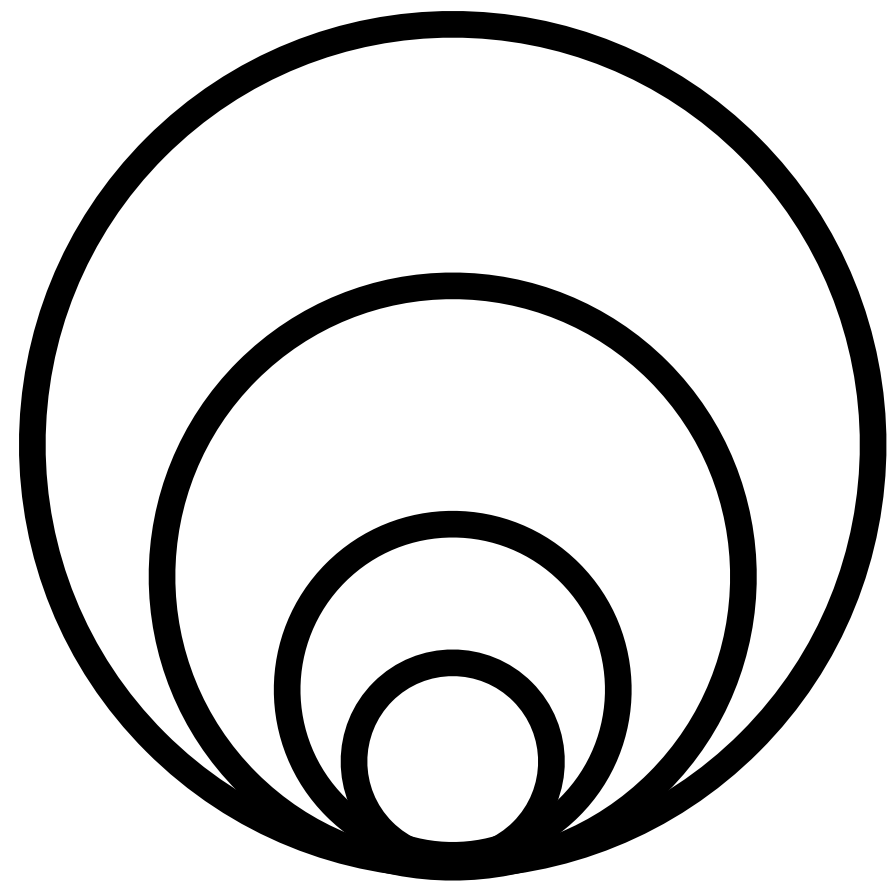
- **Node positions** — where the nodes are placed in the space?
- **Node features** — size/colour/shape?
- **Edge features** — thickness, colour?

# Node Positions

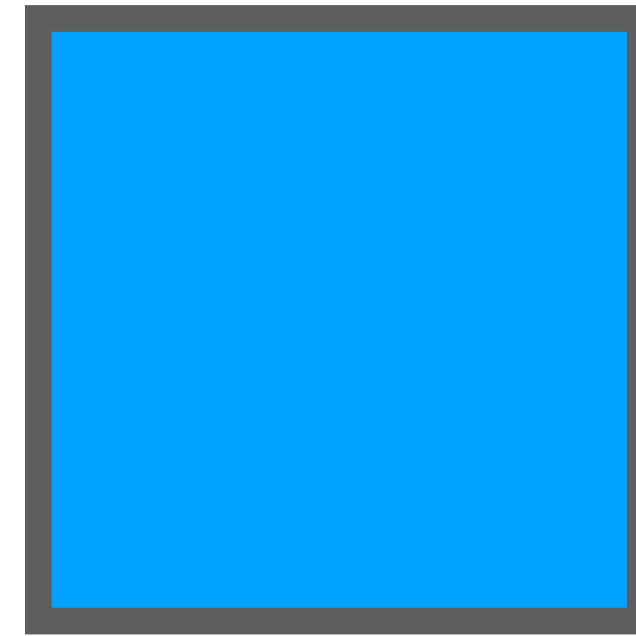
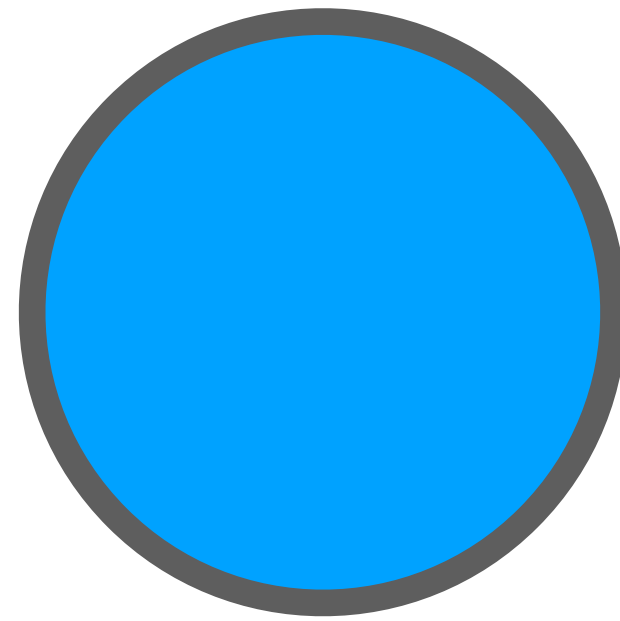
- Want to minimise **edge crossover**
- Put nodes that are **close to each other** by hops close to each other in the space
- **Layout algorithms** help with this (but are not perfect)



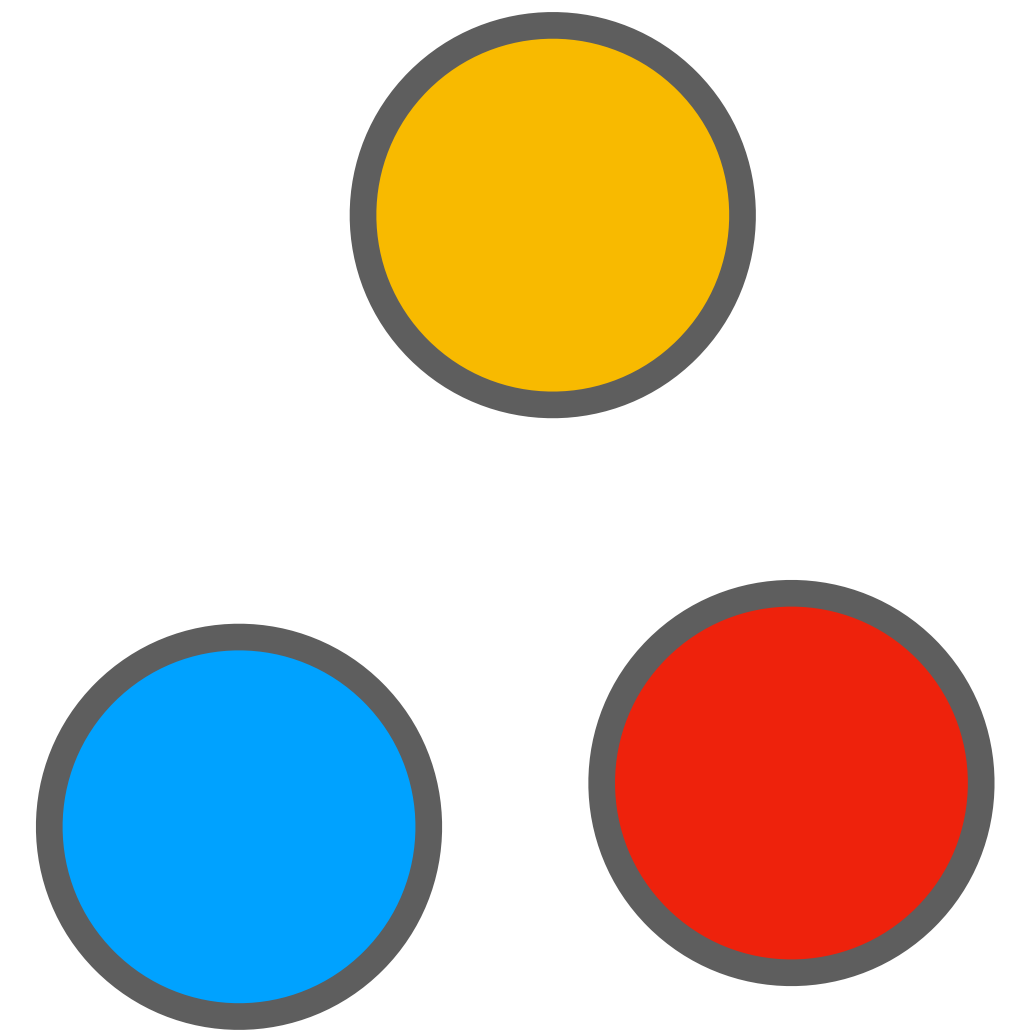
# Node Properties



**Size** (usually some centrality measure)



**Shape** (different type of nodes in the graph?)



**Colour** (usually community-related)

# Rest of tutorial: Gephi Demo

**Dataset of Twitter interactions during a conference centred around the  
#NetSci2018 hashtag, collected by Ulf Aslak**

**<https://gist.github.com/ulfaslak/2686ebe674b761e7947aacd2780b8384>**